

**A.** What is  $H^{\otimes n} \otimes H^{\otimes n}$ ?

**B.** In lecture we proved a theorem about  $H^{\otimes n} |\alpha\rangle$ . The proof had a rather large algebra step that wasn't as clear as it could be. The step becomes clearer if we re-organize the proof to be a proof by induction. So your assignment is: Prove the theorem by induction for all  $n \geq 1$ . (The base case  $n = 1$  was already done in lecture.)

**C.** In lecture we proved a theorem about  $F|\alpha\rangle|-\rangle$ . Another interpretation of that theorem is that we're demonstrating  $2^n$  eigenvectors for  $F$ . Each eigenvalue is 1 or  $-1$ , depending on exactly which  $f$  underlies  $F$ . So my question for you is: Where are the other  $2^n$  eigenvectors for  $F$ ? (Yes, it has all  $2^{n+1}$  eigenvectors.)

**D.** Here is a classical seven-bit operation:

$$|\alpha\beta\gamma\delta\zeta\eta\theta\rangle \mapsto |\alpha\rangle|\beta\rangle|\gamma\rangle|\delta\rangle|\zeta \oplus (\alpha \odot \gamma) \oplus (\alpha \odot \beta \odot \delta) \oplus (\gamma \odot \beta \odot \delta)\rangle|\eta \oplus \alpha \oplus \gamma \oplus (\beta \odot \delta)\rangle|\theta \oplus \beta \oplus \delta\rangle.$$

Is it invertible? What does it do, in English? (Hint: Analyze it from right to left.)