

There are six problems labeled A-F. The first four problems are intended to help you practice basic skills with CFGs. If you feel that you need more practice, then do more examples from the textbook.

- A. Problem 2.4b (about starting and ending with the same symbol).
- B. Problem 2.4c (about odd-length strings).
- C. Problem 2.4f (about the empty set).
- D. Problem 2.6b (about the complement of our canonical non-regular language).

Here is our CFG from class for fully parenthesized algebraic expressions:

```

<expr> ::= <var> | <num> | (<expr><op><expr>)
<var>  ::= <char> | <char><var>
<char> ::= a | ... | z | A | ... | Z | _
<num>  ::= <dig> | <dig><num>
<dig>  ::= 0 | ... | 9
<op>   ::= + | * | ^ | - | /

```

- E. Based on the CFG above, draw the parse tree for the expression

$((3 * (4 / \text{temp})) - ((x + 50) * (\text{rate} ^ \text{pow})))$

Mimic the textbook's examples in Section 2.1, with variables labeling branch nodes and terminals labeling leaf nodes. For example, the root node of your parse tree will be labeled `<expr>`. Do not take shortcuts; draw the entire tree. (For example, just the subtree corresponding to `pow` requires nine nodes.)

- F. Prove that every regular language is context-free, by showing that any regular expression can be converted into a context-free grammar that describes the same language. Hint: Use structural induction, as we did in converting regular expressions to NFAs.