Day 23 Homework CS 254

In class we proved that if  $A \leq_p B$  and  $B \in P$ , then  $A \in P$ . This first problem addresses the analogous question for NP.

A. If  $A \leq_p B$  and  $B \in NP$ , then must it be true that  $A \in NP$ ? Prove your answer.

In class, we have done two examples of specific polynomial-time mapping reductions: reducing 3SAT to CLIQUE and to VERTEX-COVER. A third example is the construction of Theorem 7.56, which reduces 3SAT to SUBSET-SUM. You are not required to read it right now, but consider doing so, because these constructions get easier as you see more of them. And this next problem asks you to do your own reduction.

B. Do problem 7.26 (which is about reducing 3SAT to  $\neq SAT$ ).