

This assignment is project work due at the end of the term.

A. In `qAlgorithms.py`, implement the following function.

```
def simon(n, f):
    '''The inputs are an integer  $n \geq 2$  and an  $(n + (n - 1))$ -qbit gate  $F$ 
    representing a function  $f: \{0, 1\}^n \rightarrow \{0, 1\}^{(n - 1)}$  hiding an  $n$ -bit
    string  $\delta$  as in the Simon (1994) problem. Returns a list or tuple of  $n$ 
    classical one-qbit states (each  $|0\rangle$  or  $|1\rangle$ ) corresponding to a uniformly
    random bit string  $\gamma$  that is perpendicular to  $\delta$ .'''
```

B. In `qAlgorithms.py`, paste the following test function. Replace the `pass` line with code that uses Simon's algorithm to make a prediction for δ . The function `reduction` in `qBitStrings.py` should help.

```
def simonTest(n):
    # Pick a non-zero delta uniformly randomly.
    delta = qb.string(n, random.randrange(1, 2**n))
    # Build a certain matrix M.
    k = 0
    while delta[k] == 0:
        k += 1
    m = numpy.identity(n, dtype=int)
    m[:, k] = delta
    mInv = m
    # This f is a linear map with kernel {0, delta}. So it's a valid example.
    def f(s):
        full = numpy.dot(mInv, s) % 2
        full = tuple([full[i] for i in range(len(full))])
        return full[:k] + full[k + 1:]
    gate = qg.function(n, n - 1, f)
    pass
    if delta == prediction:
        print("passed simonTest")
    else:
        print("failed simonTest")
        print("    delta = " + str(delta))
        print("    prediction = " + str(prediction))
```