

This is project work due at the end of the term.

**A.** In `qGates.py`, implement the following function.

```
def fourierRecursive(n):  
    '''Assumes n >= 1. Returns the n-qbit quantum Fourier transform gate T.  
    Computes T recursively rather than from the definition.'''
```

My implementation uses helper functions `fourierS`, `fourierR`, `fourierQ`, and `fourierD`, but yours is not required to.

You are not required to implement everything in terms of small gates. For example, my `fourierD` constructs  $D^{(k)}$  as a diagonal  $2^k \times 2^k$  matrix.

If you haven't implemented the original `fourier` function yet, you may not implement that function by simply calling this function. I want you to end up with two unrelated ways to compute the gate  $T$ , that we can test against each other.

**B.** In `qGates.py`, add a `fourierRecursiveTest(n)` function. It can be as simple as comparing the results of `fourier(n)` and `fourierRecursive(n)`, passing if and only if they are equal (up to numerical imprecision).