Section $16.4 \# 14,22$.
Section $16.5 \# 1 b, 9 a, 10 a$. (Notice that I'm asking about divergence and not curl.)
For these last two problems, consider the triangle in $\mathbb{R}^{2}$ whose vertices are $\vec{p}=\left(p_{1}, p_{2}\right)$, $\vec{q}=\left(q_{1}, q_{2}\right)$, and $\vec{r}=\left(r_{1}, r_{2}\right)$ in counterclockwise order. Let $\vec{F}=\langle-y / 2, x / 2\rangle$. As we have seen in class, the area of the triangle equals the line integral of $\vec{F}$ along the (counter-clockwise-oriented) boundary curve.
A. Compute the line integral of $\vec{F}$ over the line segment from $\vec{p}$ to $\vec{q}$ ( not from $\vec{q}$ to $\vec{p}$ ). Simplify your answer as much as possible.
B. Using problem A three times, give a simple expression for the area of the triangle in terms of $p_{1}, p_{2}, q_{1}, q_{2}, r_{1}, r_{2}$.

Your homework consists of the problems above. You are not expected to hand in solutions to the problems below, but of course they enhance your learning, and they might help you study for Exam D. By the way, this material is not just a math exercise; I have seen it used to solve problems in geophysics and in computer graphics.
C. Re-derive the expression for area in problem B more quickly, by using the cross product of certain vectors.

If problem C makes you feel that problems $A-B$ were a waste of time, then problems D and E might make you feel better. They show that problems A-B generalize in a way that problem C does not.
D. Extrapolating from problem B, guess an expression for the area of an $n$-sided polygon in $\mathbb{R}^{2}$, whose boundary is a simple closed curve, with vertices listed in counterclockwise order.
E. Returning to the triangle, it is possible to compute the moments $M_{y}$ and $M_{x}$ by following the same approach with a different $\vec{F}$ ?

