

On Friday Day 08, I modified this assignment to be shorter. Namely, part b of problem A is no longer required, and parts bcd of problem D are no longer required.

A. Section 20 Exercise 3a (about the metric's being a continuous function).

(Hint: I solved this problem by considering the special case $X = \mathbb{R}$ and $U = (a, b)$, drawing a picture, and using that picture to invent a proof that $d^{-1}(U)$ was open. After that, the general solution required only minor improvements to the special-case solution.)

B. Section 21 Exercise 2 (about embeddings, which are defined on page 105).

We didn't get to "limit points" in class today, but all you need to do the following exercise is the definition: If $Y \subseteq X_T$, then $x \in X$ is a *limit point* of Y if every neighborhood of x intersects Y in at least one point other than x . In other words, $x \in \overline{Y - \{x\}}$.

C. In \mathbb{R}^2 , let Y be the graph of $y = \sin(1/x)$ for $x > 0$. What are (A) the interior, (B) the closure, (C) the boundary, and (D) the set of limit points of Y ? You do not need to rigorously prove your answers, but do be careful.

D. Section 17 Exercise 19a (about boundaries).

Here's a bonus question, which you are not required to hand in: In a metric space (X, d) , recall that $B(x, \epsilon) = \{y : d(x, y) < \epsilon\}$. Is it true that $\overline{B(x, \epsilon)} = \{y : d(x, y) \leq \epsilon\}$? Prove so or give a counter-example.

Want more optional practice? Try Section 17 Exercises 2, 7, 8, 9, 20, and 19bcd. Also, study what Munkres has to say about closed subsets of a subspace Y of a space X_T .